Pearson
Edexcel

# Mark Scheme (Results)

## January 2022

Pearson Edexcel International A Level
in Statistics S2 (WST02) Paper 01

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**General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

# EDEXCEL IAL MATHEMATICS

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## General Instructions for Marking

1. The total number of marks for the paper is 75.

2. The Edexcel Mathematics mark schemes use the following types of marks:

   - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
   - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
   - **B** marks are unconditional accuracy marks (independent of M marks)
   - Marks should not be subdivided.

3. Abbreviations

   These are some of the traditional marking abbreviations that will appear in the mark schemes.

   - bod – benefit of doubt
   - ft – follow through
   - the symbol √ will be used for correct ft
   - cao – correct answer only
   - cso - correct solution only. There must be no errors in this part of the question to obtain this mark
   - isw – ignore subsequent working
   - awrt – answers which round to
   - SC: special case
   - oe – or equivalent (and appropriate)
   - dep – dependent
   - indep – independent
   - dp decimal places
   - sf significant figures
   - * The answer is printed on the paper
   - ⌐ The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.

6. If a candidate makes more than one attempt at any question:
   - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
   - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer

**<u>Special notes for marking Statistics exams (for AAs only)</u>**

- Any correct method should gain credit. If you cannot see how to apply the mark scheme but believe the method to be correct then please send to review.
- For method marks, we generally allow or condone a slip or transcription error if these are seen in an expression. We do not, however, condone or allow these errors in accuracy marks.

| Question Number | Scheme | Marks |
|---|---|---|
| 1 (a) | $X$ = faults in a week $\Rightarrow X \sim \text{Po}(6)$ | |
| | $[\text{P}(X \geqslant x) = 0.1528 \Rightarrow \text{P}(X \leqslant x-1)] = 0.8472$ | M1 |
| | Using tables $\text{P}(X \leqslant 8) = 0.8472 \Rightarrow x - 1 = 8$ | M1 |
| | $x = 9$ | A1 |
| | | (3) |
| (b) | $Y$ = faults in six weeks $\Rightarrow Y \sim \text{N}(36, 36)$ | B1 |
| | $\text{P}(Y < 32) = \text{P}\left(Z < \dfrac{31.5-36}{6}\right) \quad \left[= \text{P}(Z < -0.75)\right]$ | M1 M1 |
| | = 0.2266 awrt 0.227 | A1 |
| | | (4) |
| (c) | $W$ = Number of *poor weeks* $\Rightarrow W \sim \text{B}(50, 0.1528)$ | B1 |
| | $[\text{P}(W > 1)] = 1 - \text{P}(W \leqslant 1)$ | M1 |
| | $= 1 - \left(0.8472^{50} + 50 \times 0.1528 \times 0.8472^{49}\right)$ | dM1 |
| | = 0.99748… awrt 0.997 | A1 |
| | | (4) |

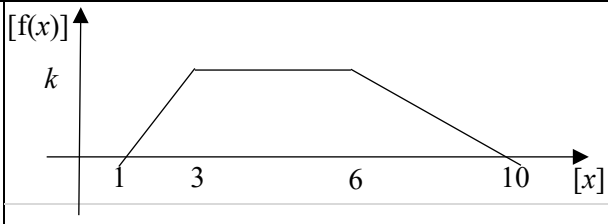
| | **Notes** | | **Total 11** |
|---|---|---|---|
| 1 (a) | **M1** | Writing or using $1 - \text{P}(X \leqslant x - 1)$ | |
| | **M1** | For 0.8472 May be implied by $x - 1 = 8$ | |
| | **A1** | $x = 9$ | |
| (b) | **B1** | Writing or using $\text{N}(36, 36)$ (May be implied by a correct standardisation expression) | |
| | **M1** | Standardising with 30.5/31/31.5/32/32.5/39.5/40/40.5/41/41.5, their mean and standard deviation (Allow ±) | |
| | **M1** | A fully correct standardisation. May be implied by ± 0.75 | |
| | **A1** | awrt 0.227 | |
| (c) | **B1** | Writing or using $\text{B}(50, 0.1528)$ | |
| | **M1** | Writing or using $1 - \text{P}(W \leqslant 1)$ (Allow any letter) | |
| | **dM1** | Dependent on using binomial.<br>Using $1 - \left[\text{P}(W = 0) + \text{P}(W = 1)\right]$ (implied by awrt 0.997 or 0.9975 or1 – awrt 0.00257)<br>Using binomial may be implied by $(1-p)^{50} + {}^{n}C_{r} \times p \times (1-p)^{49}$ where $p$ is a probability<br>Condone ${}^{n}C_{r}$ missing | |
| | **A1** | awrt 0.997 or 0.9975 | |

| Question Number | Scheme | Marks |
|---|---|---|
| 2 (a) | $\mathrm{f}(x)=\begin{cases}\dfrac{1}{4k} & -k \leqslant x \leqslant 3k \\ 0 & \text{otherwise}\end{cases}$ | M1 A1 |
| | | (2) |
| (b) | $[\mathrm{E}(X)]=k$ | B1 |
| | | (1) |
| (c) | $[\mathrm{Var}(X)]=\dfrac{(3k--k)^2}{12}=\dfrac{16k^2}{12}$ or $\left[\dfrac{x^3}{3}\ \text{"f}(x)\text{"}\right]_{-k}^{3k}-(\text{"}k\text{"})^2$ | M1 |
| | $=\dfrac{4k^2}{3}$* | A1* cso |
| | | (2) |
| (d) | $\mathrm{E}(X^2)=\mathrm{Var}(X)+\mathrm{E}(X)^2=\dfrac{4k^2}{3}+(\text{"}k\text{"})^2$ | M1 |
| | $=\dfrac{7k^2}{3}$ | A1 |
| | $\mathrm{E}(3X^2)=3\mathrm{E}(X^2)=3\times\dfrac{7k^2}{3}=7k^2$ | A1 |
| | | (3) |

| | **Notes** | **Total 8** |
|---|---|---|
| 2 (a) | **M1** | For the 1st line of the pdf including the inequality, allow use of < instead of one/both ≤ signs |
| | **A1** | Fully correct, allow use of < instead of one/both ≤ signs. Allow equivalent for the 0 otherwise. |
| (b) | **B1** | Cao |
| (c) | **M1** | Use of $\mathrm{Var}(X)=\dfrac{(\beta-\alpha)^2}{12}$ or $\left[\dfrac{x^3}{3}\ \text{"f}(x)\text{"}\right]_{-k}^{3k}-(\text{"}k\text{"})^2$ |
| | **A1* cso** | Answer is given. Correct solution only with no incorrect working. |
| (d) | **M1** | Use of $\mathrm{E}(X^2)=\mathrm{Var}(X)+\mathrm{E}(X)^2$ ft their E($X$)<br>or $\left[\dfrac{x^3}{3}\ \text{"f}(x)\text{"}\right]_{-k}^{3k}$ this integration may be seen in part (c) or part (d) |
| | **A1** | $\dfrac{7k^2}{3}$ (This must be seen in part (d)) May be implied by $7k^2$) |
| | **A1** | Cao |

| Question Number | Scheme | Marks |
|---|---|---|
| 3 (a) | We can assume breakdowns are [rare], independent events occurring at a constant rate. | B1 |
| | | (1) |
| (b) | $H_0 : \lambda = 8$ $H_1 : \lambda \neq 8$ | B1 |
| | | (1) |
| (c) | $X \sim \text{Po}(8)$ | |
| | $P(X \leqslant 2) = 0.0138$ oe $P(X \leqslant 3) = 0.0424$ oe | M1 |
| | $P(X \geqslant 14) = 0.0342$ oe $P(X \geqslant 15) = 0.0173$ oe | M1 |
| | $X \leqslant 2 \cup X \geqslant 15$ oe | A1 |
| | | (3) |
| (d) | "0.0138" + "0.0173" | M1 |
| | ="0.0311" | A1ft |
| | | (2) |
| (e) | "[4 is] not in the critical region" | M1 |
| | So there is insufficient evidence that refurbishment has changed the mean breakdown rate | A1 |
| | | (2) |

| | Notes | Total 9 |
|---|---|---|
| 3 (a) | **B1** | A correct statement which include the words independent or constant rate or singly. No context needed |
| (b) | **B1** | Both hypotheses correct. Must be attached to $H_0$ and $H_1$ in terms of $\lambda$ or $\mu$. |
| (c) | **M1** | Use of $\text{Po}(8)$ to find the lower critical value. May be implied by either 0.0138 or 0.0424 or $X \leqslant 2$ if no probabilities shown (Calculator values: 0.01375… and 0.04238…) |
| | **M1** | Use of $\text{Po}(8)$ to find the upper critical value. May be implied by 0.0342 or 0.0173 or 0.9658 or 0.9827 or $X \geqslant 15$ if no probabilities shown (Calculator values: 0.03418… and 0.01725… and 0.96581… and 0.98274…) |
| | **A1** | $X \leqslant 2$ oe [$\cup$] $X \geqslant 15$ oe Condone the use of and/or Do not allow as probability statements Allow [0, 2] or [0, 3) and [15, $\infty$] or [15, $\infty$) or (14, $\infty$] or (14, $\infty$) |
| (d) | **M1** | Adding the two probabilities for their critical region |
| | **A1ft** | 0.0311 Allow 3.11 or awrt 3.1[0] or awrt 0.031[0] ft their critical region |
| | | **NB** 3.11 or 0.0311 or awrt 3.1[0] or awrt 0.031[0] will score 2/2 |
| (e) | **M1** | A correct statement ft their critical region e.g. Do not reject $H_0$/Accept $H_0$/not significant – no context needed but do not allow contradicting non contextual comments |
| | **A1** | Correct conclusion in context. Must include rate/number of breakdown (Allow decreased for changed) |
| | | **NB** Award M1 A1 for a correct contextual statement on its own |

| Question Number | Scheme | Marks |
|---|---|---|
| 4 (a) |  | B1<br>B1 |
| | | (2) |
| (b) | $\frac{1}{2}(3+9)\times k=1$ or $\frac{1}{2}(3-1)k+(6-3)k+\frac{1}{2}(10-6)k=1$<br>or $\frac{1}{2}k\left[\frac{x^2}{2}-x\right]_1^3+k[x]_3^6+\frac{1}{4}k\left[10x-\frac{x^2}{2}\right]_6^{10}=1$ | M1 |
| | $k=\frac{1}{6}$ * | A1* cso |
| | | (2) |
| (c) | $\int_1^x \frac{1}{12}(x-1)\,dx$ or $\int \frac{1}{12}(x-1)\,dx$ and using F(1) = 0 | M1 |
| | $\int_3^x \frac{1}{6}dx+"F(3)"$ or $\int \frac{1}{6}dx$ and using "F(3) = $\frac{1}{6}$" | M1 |
| | $\int_6^x\left(\frac{5}{12}-\frac{1}{24}x\right)dx+"F(6)"$ or $\int\left(\frac{5}{12}-\frac{1}{24}x\right)dx$ and using either "F(6) = $\frac{2}{3}$" or F(10) = 1 | M1 |
| | $F(x)=\begin{cases}0 & x<1\\ \frac{1}{24}(x^2-2x+1) & 1\leqslant x\leqslant 3\\ \frac{1}{6}(x-2) & 3<x\leqslant 6\\ \frac{1}{48}(20x-x^2-52) \text{ or } 1-\frac{(10-x)^2}{48} & 6<x\leqslant 10\\ 1 & x>10\end{cases}$ | A1oe<br>A1oe<br>A1 oe<br>B1 |
| | | (7) |
| (d) | $P(X>E(X))=1-F\left(\frac{61}{12}\right)=1-0.51388...=0.4861...$ awrt 0.486 | M1 A1<br>(2) |
| (e) | Since (d) < 0.5 [the mean is greater than the median] therefore positive (skew)<br>or follow through their sketch in part (a) | M1 A1ft |
| | | (2) |

| | Notes | | Total 15 |
|---|---|---|---|
| 4(a) | **B1** | Correct shape. Must start and end on the $x$ axis | |
| | **B1** | Fully correct including 1, 3, 6, 10 and $k$. Allow $^1/_6$ for $k$ Ignore labels for $x$ and f($x$) and any extras e.g. $^k/_2$ | |
| (b) | **M1** | Setting up the area of the trapezium = 1 or 2 triangles + a rectangle = 1<br>or a fully correct integration, including limits =1 | |
| | **A1* cso** | Answer is given. Correct solution only with no incorrect working. | |

| | | |
|---|---|---|
| (c) | **M1** | For a correct method to find the 2nd line Allow in terms of $k$ |

| | | |
|---|---|---|
| | **M1** | For a correct method to find the 3rd line, ft their F(3). If using + c method then ft their F(3) = $\frac{1}{6}$<br>Allow in terms of $k$ |
| | **M1** | For a correct method to find the 4th line, ft their F(6). If using + c method then ft their F(6) = $\frac{2}{3}$<br>Allow in terms of $k$ |
| | **A1** | 2nd line correct including inequality. Allow < instead of $\leqslant$ |
| | **A1** | 3rd line correct including inequality. Allow < instead of $\leqslant$ |
| | **A1** | 4th line correct including inequality. Allow < instead of $\leqslant$ |
| | **B1** | 1st and 5th line correct. Allow "otherwise" for the range on the 1st or 5th line but not both. All 5 lines must be in terms of the same letter. |
| (d) | **M1** | For use of $1-\mathrm{F}\left(\frac{61}{12}\right)$ using the their line of F($x$) for $3 < x \leqslant 6$ . May use integration/area methods |
| | **A1** | awrt 0.486 Allow $^{35}/_{72}$ |
| (e) | **M1** | For correctly comparing part (d) with 0.5 (may be implied by a correct comparison of mean and median (5)) do not allow mean is greater than the median on its own |
| | **A1ft** | For positive skew or ft their answer to part (d) Accept "no (or negligible) skew" following a reason that "mean $\approx$ median" Allow argument based on sketch in part (a) |

| Question Number | Scheme | Marks |
|---|---|---|
| 5 (a) | B($n$, 0.045) | B1 |
| | | (1) |
| (b) | Applicants are independent (no identical twins) or the proportion/probability identified as colour blind does not change over time | B1 |
| | | (1) |
| (c) | B(120, 0.045) $\Rightarrow$ Po(5.4) | B1 |
| | $\mathrm{P}(X=5)=\dfrac{\mathrm{e}^{-5.4}\times 5.4^5}{5!}$ | M1 |
| | = 0.1728… awrt 0.173 | A1 |
| | | (3) |
| (d) | Binomial with large $n$ | B1 |
| | and very small $p$ | B1 |
| | | (2) |
| (e) | $\mathrm{H}_0: p=0.75 \quad \mathrm{H}_1: p\neq 0.75$ | B1 |
| | B(96, 0.75) $\Rightarrow$ N(72,18) | B1 |
| | $Z=\dfrac{67.5-72}{\sqrt{18}}$ or $\dfrac{x\pm 0.5-72}{\sqrt{18}}$ | M1 |
| | = –1.06066… or $\dfrac{x+0.5-72}{\sqrt{18}}<-1.96$ or $\dfrac{x-0.5-72}{\sqrt{18}}>1.96$ | A1 |
| | $\mathrm{P}(z<-1.06)=0.1444.../0.1446$ or CR < 63.2 awrt 0.144 or 0.145 | A1 |
| | There is insufficient evidence to reject $\mathrm{H}_0$ | dM1 |
| | Insufficient evidence against Jaymini's claim | A1 |
| | | (7) |
| **ALT** | Let $p$ be the probability of an applicant fail to become a pilot. | |
| | $\mathrm{H}_0: p=0.25 \quad \mathrm{H}_1: p\neq 0.25$ | B1 |
| | B(96, 0.25) $\Rightarrow$ N(24,18) | B1 |
| | $Z=\dfrac{28.5-24}{\sqrt{18}}$ or $\dfrac{x\pm 0.5-24}{\sqrt{18}}$ | M1 |
| | = 1.06066… or $\dfrac{x+0.5-24}{\sqrt{18}}<-1.96$ or $\dfrac{x-0.5-24}{\sqrt{18}}>1.96$ | A1 |
| | $\mathrm{P}(z>1.06)=0.1444.../0.1446$ or CR > 32.8 awrt 0.144 or 0.145 | A1 |
| | There is insufficient evidence to reject $\mathrm{H}_0$ | dM1 |
| | Insufficient evidence against Jaymini's claim | A1 |
| | | (7) |

| | **Notes** | **Total 14** |
|---|---|---|
| 5 (a) | **B1** | For binomial with correct parameters $n$ and 0.045 |
| (b) | **B1** | For one of the given reasons. Must have context Allow equivalent statements Do not allow number for proportion/probability |
| (c) | **B1** | Using or writing Po(5.4) |
| | **M1** | For $\dfrac{\mathrm{e}^{-\lambda}\lambda^5}{5!}$ with any value for $\lambda$ |
| | **A1** | awrt 0.173 |
| | | **NB** A correct answer with no incorrect working scores 3/3 |
| (d) | **B1** | $n$ is large (Allow number of trials for $n$) |

| | | |
|---|---|---|
| | **B1** | $p$ is small (Allow probability for $p$) |
| (e) | **B1** | Both hypotheses correct in terms of $p$ or $\pi$ Must be attached to $H_0$ and $H_1$ |
| | **B1** | For writing or using N(72, 18) (May be implied by a correct standardisation expression) |
| | **M1** | Standardising using 67.5 or 67 or 66.5 or $x \pm 0.5$ with their mean and standard deviation (Allow ±) |
| | **A1** | awrt -1.06 (may be implied by awrt 0.144 or 0.145) or a correct standardisation with ±1.96 (ignore incorrect inequality symbol and allow =) |
| | **A1** | Using a probability route: awrt 0.144 or 0.145 or critical value of $z = \pm 1.96$<br>Using a critical region route: CR < 63.2 |
| | **dM1** | Dependent on M1 A1. A correct statement – no context needed but do not allow contradicting non contextual comments. (Ignore any comparisons) |
| | **A1** | Correct conclusion in context. Must include the word claim.<br>If they give an answer that refers to the claim then they must include the words applicants (oe), and pilots. No hypotheses then A0 |
| | | **NB** Award M1 A1 for a correct contextual statement on its own |
| **ALT** | **B1** | Both hypotheses correct in terms of $p$ or $\pi$ Must be attached to $H_0$ and $H_1$ |
| | **B1** | For writing or using N(24, 18) (May be implied by a correct standardisation expression) |
| | **M1** | Standardising using 28.5 or 29 or 29.5 or $x \pm 0.5$ with their mean and standard deviation (Allow ±) |
| | **A1** | awrt 1.06 (may be applied by awrt 0.144 or 0.145) or a correct standardisation with ±1.96 (ignore incorrect inequality symbol and allow =) |
| | **A1** | Using a probability route: awrt 0.144 or 0.145 or critical value of $z = \pm 1.96$<br>Using a critical region route: CR < 32.8 |
| | **dM1** | Dependent on M1 A1. A correct statement – no context needed but do not allow contradicting non contextual comments. (Ignore any comparisons) |
| | **A1** | Correct conclusion in context. Must include the word claim.<br>If they give an answer that refers to the claim then they must include the words applicants (oe), and pilots. No hypotheses then A0 |
| | | **NB** Award M1 A1 for a correct contextual statement on its own |

| Question Number | Scheme | Marks |
|---|---|---|
| 6 (a) | A sampling distribution is **all** the **values** of a **statistic** (obtained from a random sample) and the associated **probabilities**<br>**or** the **probability distribution** of the **statistic (**under random sampling). | B1 (1) |
| (b) | $P(6)=\frac{6}{11}$ $P(7)=\frac{3}{11}$ $P(8)=\frac{2}{11}$ | B1 |
| | Totals ($T$) 12, 13, 14, 15, 16 | B1 |
| | (6, 6) (6, 7) (6, 8)<br>(7, 6) (7, 7) (7, 8)<br>(8, 6) (8, 7) (8, 8) | B1 |
| | $[P(T=12)=]\ "\left(\frac{6}{11}\right)"^2=\left[\frac{36}{121}\right]$ | |
| | $[P(T=13)=]2\times "\left(\frac{6}{11}\right)"\times "\left(\frac{3}{11}\right)"=\left[\frac{36}{121}\right]$ | M1 |
| | $[P(T=14)=]2\times "\left(\frac{6}{11}\right)"\times "\left(\frac{2}{11}\right)"+"\left(\frac{3}{11}\right)"^2=\left[\frac{33}{121}\right]$ | M1 |
| | $[P(T=15)=]2\times "\left(\frac{3}{11}\right)"\times "\left(\frac{2}{11}\right)"=\left[\frac{12}{121}\right]$ | M1 |
| | $[P(T=16)=]\ "\left(\frac{2}{11}\right)"^2=\left[\frac{4}{121}\right]$ | |
| | $T$: 12, 13, 14, 15, 16<br>$P(T=t)$: $\frac{36}{121}$, $\frac{36}{121}$, $\frac{33}{121}$, $\frac{12}{121}$, $\frac{4}{121}$ | A1 (7) |
| (c) | $E(T)="12"\times"\frac{36}{121}"+"13"\times"\frac{36}{121}"+"14"\times"\frac{33}{121}"+"15"\times"\frac{12}{121}"+"16"\times"\frac{4}{121}"$ | M1 |
| | $=\frac{1606}{121}=\frac{146}{11}=13.272...$ awrt 13.3 | A1 (2) |
| | **Notes** | **Total 10** |

| | | |
|---|---|---|
| 6 (a) | **B1** | A correct explanation with the words in bold |
| (b) | **B1** | Correct probabilities – may be seen in an equation or implied by a correct probability for $T = 14$ |
| | **B1** | All 5 totals correct with no extras |
| | **B1** | All 6 basic combinations correct, either seen or used (may be implied by correct probailities)<br>Allow S for 6, M for 7 and L for 8 |
| | **M1** | Correct method for one probability ft their P(6), P(7) and P(8) If these are not stated then they must be correct |
| | **M1** | Correct method for three of the five probabilities ft their P(6), P(7) and P(8) If these are not stated then they must be correct |
| | **M1** | Correct method for all five probabilities ft their P(6), P(7) and P(8) If these are not stated then they must be correct or 5 probabilities that add up to 1 |
| | **A1** | cao Need not be in a table but probabilities must be attached to the correct total |
| (c) | **M1** | Use of $\sum tP(T=t)$ two or more products ft their table |
| | **A1** | awrt 13.3 (Allow $\frac{146}{11}$ oe) |

| Question Number | Scheme | Marks |
|---|---|---|
| 7 (a) | $P(L \geqslant 4.5) \Rightarrow P(A \geqslant 20.25)$ | |
| | $P(A \geqslant 20.25) = (30 - 20.25) \times \frac{1}{20}$ | M1 |
| | $= 0.4875$ | A1 |
| | | (2) |
| (b) | $\text{Var}(L) = E(L^2) - E(L)^2$ | |
| | $[E(L^2) = E(A)] = 20$ | B1 |
| | $g(L) = \begin{cases} \frac{L}{10} & \sqrt{10} \leqslant L \leqslant \sqrt{30} \\ 0 & \text{otherwise} \end{cases}$ | |
| | $E(L) = E(\sqrt{A}) = \frac{1}{20}\int_{10}^{30} \sqrt{a}\ \mathrm{d}A$ $\quad E(L) = \frac{1}{10}\int_{\sqrt{10}}^{\sqrt{30}} L^2\ \mathrm{d}L$ | M1 |
| | $= \frac{1}{20}\left[\frac{2}{3}a^{\frac{3}{2}}\right]_{10}^{30}$ $\quad \frac{1}{10}\left[\frac{l^3}{3}\right]_{\sqrt{10}}^{\sqrt{30}}$ | A1 |
| | $= 4.4231\ldots$ | A1 |
| | $\text{Var}(L) = \text{"20"} - (\text{"4.4231..."})^2$ | M1 |
| | $= 0.4358\ldots$ awrt 0.436 | A1 |
| | | (6) |

| | Notes | Total 8 |
|---|---|---|
| 7 (a) | **M1** | $(30 - 20.25) \times \frac{1}{20}$ |
| | **A1** | cao (Allow 0.488 or $\frac{39}{80}$) |
| (b) | **B1** | For 20 |
| | **M1** | Attempt to integrate $\frac{1}{20}\int_{10}^{30} \sqrt{a}\ \mathrm{d}A$ or $\frac{1}{10}\int_{\sqrt{10}}^{\sqrt{30}} L^2\ \mathrm{d}L$ Ignore limits and accept any letter |
| | **A1** | Fully correct integration. Accept any letter. Must have limits |
| | **A1** | 4.42 or better |
| | **M1** | Use of $\text{Var}(L) = E(L^2) - E(L)^2$ ft their $E(L^2)$ and $E(L)$ provided Var $(L) > 0$ |
| | **A1** | awrt 0.436 |